Name: $\qquad$ Student ID: $\qquad$
Answer each question. For True/False statements, circle T or F.
Linear algebra review:
Let $A$ be an $m \times n$ matrix, and let $\vec{b}$ be a vector in $\mathbb{R}^{m}$.
For $\vec{u}, \vec{v} \in \mathbb{R}^{n}$, the notation $\vec{u} \leq \vec{v}$ means $u_{1} \leq v_{1}, u_{2} \leq v_{2}, \ldots, u_{n} \leq v_{n}$.

1. The equation $A \vec{x}=\vec{b}$ has a solution if and only if $\vec{b}$ is a linear combination of the columns of $A$. $\mathbf{T} / \mathbf{F}$
2. $V=\{\vec{x} \mid A \vec{x}=\vec{b}\}$ is infinite if and only if $\operatorname{dim}(N u l(A))>0$. $\mathbf{T} / \mathbf{F}$
3. If $m<n$, then $V=\{\vec{x} \mid A \vec{x}=\vec{b}\}$ is infinite. $\mathbf{T} / \mathbf{F}$
4. $\{\vec{x} \mid A \vec{x} \leq \vec{b}\}$ is a subspace of $\mathbb{R}^{n}$. $\mathbf{T} / \mathbf{F}$
5. $\{\vec{x} \mid A \vec{x} \leq \overrightarrow{0}\}$ is a subspace of $\mathbb{R}^{n}$. $\mathbf{T} / \mathbf{F}$
6. $\{\vec{x} \mid A \vec{x}=\vec{b}\}$ is a subspace of $\mathbb{R}^{n}$. $\mathbf{T} / \mathbf{F}$
7. $\{\vec{x} \mid A \vec{x}=\overrightarrow{0}\}$ is a subspace of $\mathbb{R}^{n}$. $\mathbf{T} / \mathbf{F}$
8. Homogeneous equations $A \vec{x}=\overrightarrow{0}$ always have a solution. T/F
9. If $\vec{p}$ is a solution to $A \vec{x}=\vec{b}$, then $\vec{p}+\vec{v}$ is also solution to $A \vec{x}=\vec{b}$ for any solution $\vec{v}$ to $A \vec{x}=\overrightarrow{0}$. $\mathbf{T} / \mathbf{F}$
10. Row operations on the augmented matrix $[A \vec{b}]$ are equivalent to multiplying on both sides of $A \vec{x}=\vec{b}$ by an elementary matrix. $\mathbf{T} / \mathbf{F}$
11. Suppose $A$ is invertible. We can use row operations to transform the augmented matrix $[A \vec{b}]$ into the matrix $\left[I_{n} \vec{p}\right]$ for some $\vec{p}$ in $\mathbb{R}^{n}$. T/F
12. Suppose $m<n$ and the first $m$ columns of $A$ are linearly independent. We can use row operations to transform the augmented matrix $[A \vec{b}]$ into the matrix $\left[I_{m} D \vec{p}\right]$ for some $m \times(n-m)$ matrix $D$ and some $\vec{p}$ in $\mathbb{R}^{n}$. T / F
13. $\vec{x}=\left[\begin{array}{c}\vec{p} \\ \overrightarrow{0}\end{array}\right]$ is a solution to $A \vec{x}=\vec{b}$ in the previous problem. $\mathbf{T} / \mathbf{F}$
14. Consider linear equation $A \vec{x}=\vec{b}$. If the rows of $A$ are rearranged, then the order of the variables in $\vec{x}$ must be rearranged. $\mathbf{T} / \mathbf{F}$
15. Consider linear equation $A \vec{x}=\vec{b}$. If the columns of $A$ are rearranged, then the order of the variables in $\vec{x}$ must be rearranged. $\mathbf{T} / \mathbf{F}$
